### Random walks on Graphs, Background

Random walks on graphs are a fundamental concept in network science and social computing. They are mathematical models used to describe how an entity (e.g., a person, information, or a disease) moves through a graph (a network of interconnected nodes or vertices). This concept has broad applications in understanding social networks, information diffusion, recommendation systems, and various other aspects of social computing.

# **Graph Representation:**

A graph is composed of nodes (vertices) and edges (connections) that link nodes. In social computing, nodes typically represent entities like individuals, web pages, or social media users, while edges represent relationships or interactions between them.

# **Random Walks on Background:**

A random walk is a stochastic process where an entity starts at a particular node and moves to adjacent nodes based on a set of probabilistic rules. The entity's path is determined by a sequence of random choices.

# Markov Chains:

Random walks are often modeled as Markov chains, a mathematical framework where the probability of transitioning from one node to another depends only on the current node and not on previous steps. Markov chains are memoryless.

# **Transition Probabilities:**

Transition probabilities are key to random walks. They specify the likelihood of moving from one node to another. These probabilities can be uniform, weighted based on edge attributes, or personalized according to the entity's preferences or behavior.

# **Applications in Social Computing:**

PageRank Algorithm: Google's PageRank algorithm uses random walks on the web graph to rank web pages. It measures the importance of a page based on the probability that a random walker will visit that page.

Recommendation Systems: Random walks are used in recommendation algorithms to discover patterns in user behavior and provide personalized recommendations. For instance, they can be used to identify products that are frequently purchased together.

Community Detection: Random walks help identify communities or clusters of nodes in a social network by observing the tendency of random walkers to stay within a community.

Information Diffusion: Understanding how information or influence spreads through a network often involves modeling random walks. For example, studying how news articles go viral on social media.

### **Example in Social Computing:**

Now, let's consider a practical example in social computing:

Suppose we have a social network graph where nodes represent users, and edges represent connections or friendships between users. We want to study how information spreads within this network through random walks.

Starting Point: We begin with a starting user (Node A) who shares a piece of information (e.g., a post, a news article) with their immediate friends (Nodes B, C, and D).

Random Walks: To understand how this information spreads, we initiate random walks from each of the initial recipients (Nodes B, C, and D). These random walks represent the way in which the shared information is disseminated through the network.

Propagation: During these random walks, users may further share the information with their friends, and the process continues. Some users may share the information widely, while others may not share it at all.

Analysis: By analyzing the paths taken by these random walks, we can gain insights into how quickly and to what extent the information spreads through the social network. This information can be useful for various purposes, such as optimizing the placement of advertisements or understanding the virality of content.

Random walks on graphs provide a mathematical framework for modeling and simulating various processes, including information propagation, recommendation systems, and network analysis, in the context of social computing. They help us understand the dynamics of complex networks and how entities move or interact within them.